Week 2 - Wednesday

COMP 1800

Last time

- What did we talk about last time?
- π
- math library
- Archimedes' approximation
- Leibniz's approximation

Questions?

Back to π

Problem solving

- The famous mathematics educator George Pólya outlined a series of steps for solving problems:
 - **1**. Understand the problem
 - 2. Make a plan
 - 3. Execute the plan
 - 4. Look back and reflect

John Wallis

- John Wallis was a 17th century British mathematician who is believed to have come up with the ∞ symbol for infinity
- Of course, he also found an approximation for π

$$\frac{\pi}{2} = \frac{2}{1} \cdot \frac{2}{3} \cdot \frac{4}{3} \cdot \frac{4}{5} \cdot \frac{6}{5} \cdot \frac{6}{7} \cdot \frac{8}{7} \cdots$$



Wallis approximation

$$\frac{\pi}{2} = \frac{2}{1} \cdot \frac{2}{3} \cdot \frac{4}{3} \cdot \frac{4}{5} \cdot \frac{6}{5} \cdot \frac{6}{7} \cdot \frac{8}{7} \cdots$$

- As with Leibniz, we will use the Accumulator Pattern
- Although the Accumulator Pattern often adds things up, we'll be multiplying stuff as we go
 - When summing, we start with o
 - When multiplying, we start with 1
- Note that both the numerator and the denominator are used twice in a row before increasing by two
 - But they change on opposite turns!
- How can we apply Pólya's problem solving approach?

Selection Statements

Behold!

• To make choices in our program, we can use an **if**-statement:

x = 4
if x < 5:
 print('x is small!')</pre>

- **x** is small will only print out if **x** is less than 5
- In this case, we know that it is, but x could come from user input or a file or elsewhere

Anatomy of an if



Note: The colon after the condition and the indentation before the statement are **required**

Conditions in the if

- Any statement that evaluates to a Boolean is legal
- Examples:
 - x <= y
 - True
 - s == 'Help me!' and z < 4
- In actual fact, almost anything can be used for the condition
 - Integers and floating-point values are considered True as long as they aren't zero
 - Most strings (except the empty string ' ') are considered True
 - Avoid using things that aren't Booleans, since it's confusing

Comparison

- The most common condition you will find is a comparison between two things
- In Python, that comparison can be:
 - equals
 - != does not equal
 - < less than
 - Iess than or equal to
 - s greater than
 - s= greater than or equal to
- These are called relational operators

Equals

- You can use the == operator to compare any two things of the same type
- Different numerical types can be compared as well (3 ==
 - 3.0)

x = 3
if x == 4:
 print('This doesn't print')



- Any place you could have used the == operator, you can use the != operator
- If == gives True, the != operator will always give False, and vice versa
- If you want to negate a condition, you can always use the not operator

is the same as

if
$$not(x == 4)$$
:



- Remember, a single equal sign (=) is the assignment operator (think of a left-pointing arrow)
- A double equals (==) is a comparison operator
- Assigning variables in if statements is not allowed

```
y = 10
if y = 6:  # syntax error
print('Oh, no!')
```

```
b = False
if b = False: # syntax error
print('Not this?')
```

Less Than (or Equal To)

- Inequality is very important in programming
- You may want to take an action as long as a value is below a certain threshold
- For example, you might want to keep bidding at an auction until the price is greater than what you can afford

```
if x <= 4:
    print('x is less than 5')</pre>
```

Watch for strict inequality (<) vs. non-strict inequality (<=)

Greater Than (or Equal To)

- Just like less than or equal to, except the opposite
- Note that (because of the All-Powerful Math Gods) the opposite of <= is > and the opposite of >= is <</p>
- Thus,
 - not($x \le y$) is equivalent to (x > y)
 - not($x \ge y$) is equivalent to (x < y)

and and or

- You can also have multiple Boolean conditions in an if statement
- You can join them together with:
 - and (which results in a True value only if both the conditions it joins are True)
 - or (which result in a True value if either of the conditions it joins are True)

if attempts < 5 and password == 'open sesame':
 print('You know the secret!')</pre>

Another useful library

- The random library lets us produce random numbers
 It has two functions that will be useful to us:
 - randint (a, b): Returns a random integer n where $a \le n \le b$
 - random(): Returns a random floating-point value from [0, 1)
- To use them, import random and then call the functions qualified by random followed by a period:

```
import random
```

```
dice = random.randint(1, 6)
```

```
percentage = random.random()
```

Monte Carlo approximation of $\boldsymbol{\pi}$

- We can do something called a Monte Carlo approximation of π
- We "throw" darts at a 1 x 1 square in the upper right corner of a circle with radius 1
- We count the ones that fall inside the circle and divide by the total darts thrown
- That fraction is an estimation of the area of one fourth of the circle
- By multiplying by 4, we approximate π



Monte Carlo approximation function

 Here is a function that performs the Monte Carlo approximation:

```
import random

def monteCarlo(darts):
    hits = 0
    for i in range(darts):
        x = random.random()
        y = random.random()
        if x*x + y*y <= 1.0: # see if dart is in circle
            hits += 1
    return 4.0 * hits / darts
</pre>
```



Upcoming

Next time...

- More on selection statements
- Visualization of Monte Carlo simulation
- We'll mostly have work time for assignments
 - Assignment 1 is due Friday by midnight
 - Assignment 2 will be available to work on as well

- 20 employers in the fields of Engineering and Computer Science
- 20 alumni members attending
- Free professional LinkedIn headshots
- Plenty of food and great conversations
- Build new connections on LinkedIn
- Door prizes
- Network with people in your field
- Learn about possible internships
- Gain new insights about your major
- Required event for all sophomores

ENGINEERING PROFESSIONAL DEVELOPMENT

SEPTEMBER 7, 5PM-7.30PM, @ THE POINT

CAREER JUMPSTART:

ENGINEERING & COMPUTER SCIENCE

Come and network with engineering and computer science alumni and business partners and learn how to be successful in your strategic job and internship search









- Review Chapter 2 of the textbook
- Emergency elections for CS Club
 - Do you want to have a voice in CS Club?
 - Come vote at 4 p.m. this Wednesday, August 30 in Point 113!